

202

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Second Year Bcom - Semester IV
End semester Examination – April 2016
STATISTICAL TECHNIQUES

Duration: 2 hours

Max. Marks: 80

- Instructions:** 1) All questions are compulsory (choice is internal)
2) Start each new question on a fresh page
3) Figures to the right indicate full marks
4) Programmable Calculators not allowed
5) Log tables and graph papers will be supplied on request.

Q.1 Attempt the following:

- a) Illustrate and distinguish between positive and negative correlation (3)
- b) Of the 12 Accounts held in a file, four contain procedural error in posting account balances. If an auditor samples two accounts at random, what is the probability that:
- i) No. error occurs (6)
- ii) At least one will contain an error? (6)
- c) From a well shuffled pack of cards one card is drawn at random. Find the probability that it is
- i) an ace card, ii) Spade card and iii) King of hearts or diamond card. (7)

OR

Q.I Attempt the following:

- x) Explain scatter diagram. (3)
- y) Suppose that in key punching of 80 columns IBM cards the mean of no. of mistakes per card is 0.3. What % of cards will have :
- i) No mistakes (6)
- ii) Two mistakes. (6)
- z) Given $P(A) = 0.3, P(B) = 0.5, P(A \cap B) = 0.2$, find $P(A \cup B)$ and $P(\overline{A \cup B})$. (7)

Q.2 Attempt the following:

- a) Define 1) Independent events and 2) Conditional events. (3)
- b) For the following data calculate Spearman's Rank correlation coefficient. (6)

x	10	12	15	17	19	7
y	12	15	16	18	24	42

- c) Draw a suitable control chart for the following data pertaining to the no. of foreign coloured threads (considered as defects) in 15 pieces of cloth of 2 X 2 m of a certain make of synthetic fibre and state the conclusion. (7)
- 7, 12, 3, 20, 21, 5, 4, 3, 10, 8, 0, 9, 6, 7, 20

OR

Q.II Attempt the following:

- x) Define 1) Random experiment 2) Mutually exclusive events. (3)

- y) The coefficient of rank correlation of marks obtained by 9 students was calculated to be 0.4. It was later discovered that the value of the difference between the ranks for one student was written wrongly as 6 instead of 8. Find the correct value of coefficient of rank correlation. (6)
- z) Five samples, each of size 4 are drawn from a population and the readings obtained from them are as follows: (7)

Sample No.:	S_1	S_2	S_3	S_4	S_5
Fraction defectives:	0.46	0.54	0.51	0.46	0.53

Find the control limits and draw P-chart. State whether system is in control or not

Q.3 Attempt the following:

- a) Write a short note on stratified sampling. (3)
- b) Find the two regression equation for the following data: (6)
- $$\sum X = 20, \sum Y = 11.58, \sum X^2 = 90, \sum Y^2 = 27.03, \sum XY = 47.13, n = 5$$
- c) If a random sample of size 20 from a normal population with S. D. = 5.2 show a mean of 16.9, test at 5% level of significance that the population mean is 15.5. Also calculate 99% confidence limit for mean. (7)

OR

Q.III Attempt the following:

- x) Write a short note on purposive sampling. (3)
- y) The two regression equations are $10x + 3y - 62 = 0$ and $6x + 5y - 50 = 0$. Identify the regression of x and y. Hence find \bar{x} , \bar{y} and γ and if $\sigma_x = 2$ find σ_y . (6)
- z) i) A sample of 600 persons selected at random from a large city, gives the result that males are 53%. Is there a reason to doubt the hypothesis that males and females are in equal no. in city. (4)
- ii) In a sample survey of 1000 housewives in a city 23% prefer a particular brand of a pressure cooker. Find 99% confidence limit for the percentage of all housewives in the city preferring that brand of cooker. (3)

Q.4 Attempt the following:

- a) State the condition under which Binomial distribution is used. (3)
- b) Determine the mostly likely salary of husband when wife's salary is Rs.1500. (6)

Wife's salary:	700	800	1200	1400	1700	1900
Husbands Salary:	800	1000	2000	2100	1300	2400

- c) Six samples of Size 4 each were drawn and the range of each sample is noted down. Find the CL, UCL and LCL. Also draw the control chart for range and comment. (7)
- (Given $D_3 = 0, D_4 = 2.282$ for the sample of size 4)

Sample :	S_1	S_2	S_3	S_4	S_5	S_6
Range(R):	0.2	0.1	0.56	0.22	0.14	0.21

OR

Q.IV Attempt the following:

- x) For a Poisson distribution $P(x = 0) = e^{-0.4}$. Find mean and standard deviation and $P(x = 1)$. (3)

- y) From the following table showing age of cars of a certain make and annual maintenance costs, obtain the regression equation for costs related to age. (6)

Age of Cars:	2	4	6	7	8	10	12
Annual cost:	1000	1400	1800	1900	1700	2100	2000

Estimate the approximate cost of maintaining 3 years old car of the same make.

- z) Six samples of size 4 each are drawn and then mean and range for each sample is noted down. Find the CL, UCL, LCL for the system and draw the control chart \bar{X} , Also check whether the system is in control ($A_2 = 0.729$ for size 4). (7)

Sample	S_1	S_2	S_3	S_4	S_5	S_6
Mean	1.35	2.51	1.8	2.39	1.48	2.11
Range	0.3	0.5	0.4	0.6	0.3	0.7

Q.5 Attempt the following:

- a) Explain the terms 1) Point estimate and 2) Interval estimate. (3)
 b) A normal distribution has mean of 20 and S.D. = 4. Find the probability of
 i) $P(20 < x < 23)$
 ii) $P(17 < x < 19)$

(Area under the standard normal curve from $t = 0$ to $t = 0.75$ is 0.2734 and $t = 0$ to $t = 0.25$ is 0.0987) (6)

- c) i) Two cards are drawn from a pack of cards without replacements. Find the probability that the cards are 1) both kings 2) An ace and a queen (4)
 ii) For a bivariate data $b_{xy} = \frac{9}{4}$, $b_{yx} = \frac{4}{25}$, $\sigma_x = 15$ Find the values of γ and σ_y . (3)

OR

Q.V Attempt the following:

- x) Explain 1) Level of significance and 2) Test of significance. (3)
 y) The mean yield of one plot is 662 kilos with a S.D of 32 kilos. Assuming normal distribution, how many one acre plots in a batch of 1000 plots would you expect to have yield:
 i) Over 700 kilos
 ii) Below 650 kilos

(Area under the standard normal curve for $t = 0$ to $t = 1.19$ is 0.3830, and $t = 0$ to $t = 0.38$ is 0.1480). (6)

- z) i) A player tosses a coin twice. He wins Rs.8 if 2 heads occur, Rs.3 if one head occurs and loses Rs.5 if no head occurs. Find his expected gain. (4)
 ii) Karl Pearsons co-efficient of correlation between two variables x and y is 0.521, their covariance is 7.8. If variance of x is 16. Find the standard deviation of y . (3)