

Vidya Vikas Mandal's
Shree Damodar College of Commerce & Economics
FY BCA, Semester I, Semester End Examination, October 2019
SUBJECT: Basic Mathematics

Timing: 2 Hours

Marks: 50

Instructions:

1. All questions are compulsory.
2. Figures to the right indicate maximum marks.
3. Start each question on fresh page.

Q1. Attempt the following:

A) Answer the following:

[1x5=5 Marks]

- i) Find the GCD of 414 and 662.
- ii) If $\sqrt{2n} = 64$, find n .
- iii) Find the distance between (3, 1) and (7, 4).
- iv) In an A.P. if $a=6$, $d=7/19$. Find t_{20} .
- v) If $a=2+7i$ and $b=5-12i$, find $a+b$.

B) Answer the following:

[1x5=5 Marks]

- i) Convert 200° into radian measure
- ii) If set $A = \{2, 4, 6\}$ and set $B = \{1, 3\}$, find their Cartesian product $A \times B$.
- iii) Differentiate the functions, $y = \cos x$ and $y = \cot x$
- iv) If for a G.P. $a=2$ and $r=3/2$, find t_3 .
- v) Find the height of right triangle whose base is 12cm, and its area is 36cm^2 .

Q2. Answer any two of the following questions:

[5x2=10 Marks]

- A) Solve for x , $\log_x(8x - 3) - \log_x 4 = 2$
- B) Find volume of hemisphere whose surface area is 50cm^2 .
- C) Use De Moivre's theorem to prove $\sin 2\theta = 2 \sin \theta \cos \theta$

Q3. Answer any two of the following questions:

[5x2=10 Marks]

- A) Find the sum to n terms of the series $4+44+444+\dots$

B) Show that $\frac{\sin \theta}{1 - \cot \theta} + \frac{\cos \theta}{1 - \tan \theta} = \sin \theta + \cos \theta$.

C) Find the domain and range of the function:

$$f(x) = \sqrt{(2x + 4)}.$$

Q4. Answer any two of the following questions:

[5x2=10 Marks]

A) Examine if the following function is continuous or not, at $x=1$. In case the function is discontinuous state whether the discontinuity is of removable, and if removable redefine the function suitably to make it continuous.

$$f(x) = \begin{cases} \frac{x^2 - 4x + 3}{x^2 - 1} & x \neq \pm 1 \\ 2 & x = \pm 1 \end{cases}$$

B) Differentiate the following w.r.t. x :

$$y = 3x^2 \log x$$

C) A wire in form of circle of radius 3.5m is bent in form of rectangle whose length and breadth are in ratio 6:5. What is the area of rectangle?

Q5. Answer any two of the following questions:

[5x2=10 Marks]

A) Find the cofactor matrix of $A = \begin{bmatrix} 1 & 0 & 2 \\ 2 & 3 & 3 \\ 5 & 7 & 4 \end{bmatrix}$.

B) Evaluate the following integral:

$$\int \frac{2x^2 + 4x + 5}{x}$$

C) Find $f \circ g$ and $g \circ f$ for the following functions:

i) $f(x) = x^2$, $g(x) = x-7$.

ii) $f(x) = 3x-9$, $g(x) = x+2$